		YTÜ Physics Department 2015-2016 Fall	Exam Date : 19.12.2015		Exam Time : 90 min.		
FIZ1001 Physics-1 Midterm Exam 2			P.1	P.2	P.2	P.4	TOTAL
Name Surname							
Registration No							
Department							
Group No	Exam Hall	Signature of the Student	<p>The 9<sup>th</sup> article of Student Disciplinary Regulations of YÖK Law No.2547 states "<i>Cheating or helping to cheat or attempt to cheat in exams</i>" de facto perpetrators takes one or two semesters suspension penalty. Calculators are not allowed. Do not ask any questions about the problems. There will be no explanations. Use the allocated areas for your answers and write legible.</p>				
Lecturer's Name Surname							

**PROBLEM 1:** A particle of mass  $m$  moving with a velocity of  $\vec{v}_1 = v_1 \hat{i}$  collides with a target particle of mass  $2m$  that is initially at rest at  $x = d$  as shown in Figure-1 just before the collision. After the collision (Figure-2), the mass  $m$  moves with the velocity of  $\vec{v}'_1 = \frac{v_1}{2} \hat{j}$  at an angle of  $\theta = 90^\circ$  with respect to the original line of motion.

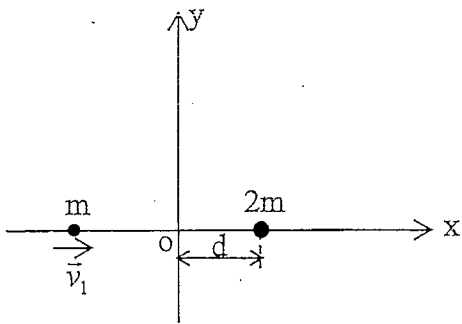


Figure-1: Before the collision

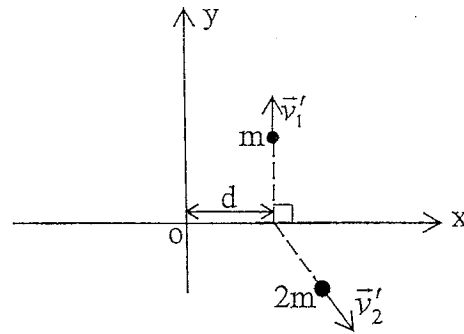


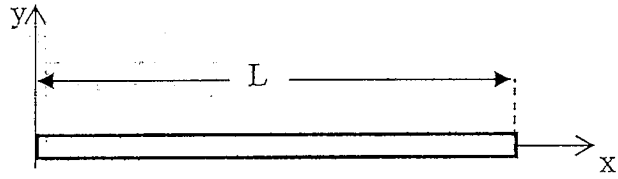
Figure -2: After the collision

a) Find the velocity  $\vec{v}'_2$  of the mass  $2m$  after the collision.

c) Define the type of the collision and explain the reason.

b) Calculate the velocity of the center of mass of the particles after the collision.

**PROBLE 2:** Consider a non-uniform rod of mass  $M$  and length  $L$  placed along the  $x$ -axis with one end at the origin, as shown in the figure. Linear mass density of the rod varies with  $x$  according to the expression  $\lambda = Ax^2$  ( $A$  is a positive constant).



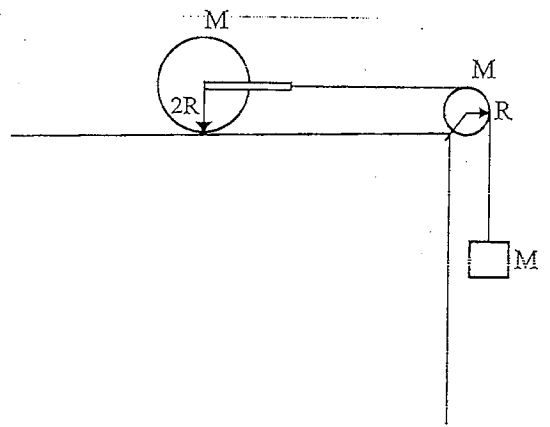
a) Find the total mass  $M$  of the rod in terms of  $A$  and  $L$ .

b) Find the position of the center of mass of the rod.

c) Calculate the moment of inertia of the rod about  $y$ -axis in terms of  $M$  and  $L$ .

d) Calculate the moment of inertia about an axis perpendicular to the rod and passing through its center of mass in terms of  $M$  and  $L$  *by using parallel axis theorem*.

**PROBLEM 3:** A uniform, solid cylinder with mass  $M$  and radius  $2R$  rests on a horizontal tabletop. A string is attached by a yoke to a frictionless axle through the center of the cylinder so that the cylinder can rotate about the axle. The string runs over a disk-shaped pulley with mass  $M$  and Radius  $R$  that is mounted on a frictionless axle through its center. A block of mass is suspended from the free end of the string (the figure). The string doesn't slip over the pulley surface, and the cylinder rolls without slipping on the tabletop. (For solid cylinder and pulley with mass  $M$  and radius  $R$  rotating around the axis through its center is;  $I = \frac{1}{2}MR^2$ ).



a) Draw free-body diagram and write the equation of motion for each mass.

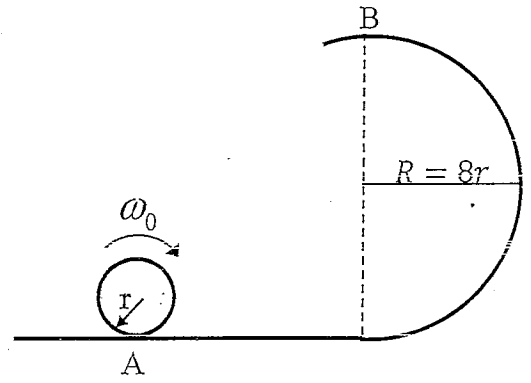
b) Find the **magnitude of the acceleration of the block** after the system is released from rest.

For mass M:

For cylinder:

For pulley:

**PROBLEM 4 : i)** A solid sphere of mass  $M$  and radius  $r$  rolls without slipping along the horizontal track (point A) with the angular speed  $\omega_0$  as shown in figure. What is the value of  $\omega_0$  so that the sphere completes the loop of radius  $R = 8r$  (passing through point B)?  
(Moment of Inertia of solid sphere;  $I = \frac{2}{5}Mr^2$ )



**ii)** A particle of mass  $m = 1\text{kg}$  has the velocity of  $\vec{v} = 2\hat{i} - \hat{k}$  and the position vector of  $\vec{r} = \hat{i} - 4\hat{j} + 2\hat{k}$  relative to the origin. Find the **angular momentum vector** and **its magnitude** relative to the origin.