

Question Sheet	AAAAAA	27/12/2024 18.30-20.10	100 min
Name	The 9th article of Student Disciplinary Regulations of YÖK Law No.2547 states “ Cheating or helping to cheat or attempt to cheat in exams ” de facto perpetrators take one or two semesters suspension penalty. Students are NOT permitted to bring calculators, mobile phones, smart watches and/or any other unauthorized electronic devices into the exam room.		
Surname			
Student No			
Group/Saloon			
Signature			

θ	0°	30°	37°	45°	53°	60°	90°	
\sin	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1	$g = 10 \text{ m/s}^2$
\cos	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0	$\pi = 3$

$$\vec{F}_{cons} = -\frac{dU}{dr} \hat{r}; W_{cons} = -\Delta U; U = mgy; U = \frac{1}{2}kx^2; \vec{F}_{net} = \frac{d\vec{p}}{dt}; \vec{p} = m\vec{v}; \vec{I} = \Delta\vec{p} = \vec{F}\Delta t; f_s \leq \mu_s n;$$

$$f_k = \mu_k n; \vec{\omega} = \frac{\Delta\theta}{\Delta t}; \vec{\alpha} = \frac{\Delta\vec{\omega}}{\Delta t}; \vec{\omega} = \frac{d\vec{\theta}}{dt}; \vec{\alpha} = \frac{d\vec{\omega}}{dt}; \vec{\omega} = \vec{\omega}_0 + \vec{\alpha}t; \theta = \theta_0 + \vec{\omega}_0 t + \frac{1}{2}\vec{\alpha}t^2; F = -kx;$$

$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0); v = r\omega; a_t = r\alpha; \vec{r}_{cm} = \frac{\sum m_i \vec{r}_i}{\sum m_i}; \vec{r}_{cm} = \frac{\int \vec{r} dm}{\int dm}; \vec{\tau} = \vec{r} \times \vec{F}; \vec{\tau}_0 = I_0 \vec{\alpha}; I = \int r^2 dm;$$

$$P = \vec{\tau} \cdot \vec{\omega}; W = \int \vec{\tau} \cdot d\vec{\theta}; \bar{P} = \frac{\Delta W}{\Delta t}; W = \Delta U + \Delta K; I_{disc} = \frac{1}{2}mr^2; I_{sphere} = \frac{2}{5}mr^2; I_{rod} = \frac{1}{12}mL^2$$

Sorular 1-3

The potential energy of a particle, given in J, is expressed as: $U(x, y) = (1 - x^3)^2 + \frac{1}{2}y^2 + \frac{1}{2}x^2y^2$.

1) What are the components of the force acting on the particle, expressed in N?

- A) $F_x = -(6x + 9x^8 - xy^2); F_y = y(x^2 - 1)$
- B) $F_x = -(6x + 6x^4 + xy^2); F_y = y(1 - x^2)$
- C) $F_x = (6x^2 - 6x^5 - xy^2); F_y = -y(1 + x^2)$**
- D) $F_x = (3x^2 + 9x^8 - 2xy^2); F_y = y(1 - x^2)$
- E) $F_x = -(3x^2 + xy^2); F_y = -y(1 + x^2)$

2) At which position along the y-axis is the particle in equilibrium?

- A) $y = -1$
- B) $y = 0$**
- C) $y = \sqrt{1 - x^2}$
- D) $y = 1$
- E) $y = -\sqrt{1 - x^2}$

3) If the force vector is $\vec{F} (2,3)$ which of the following correctly represents it in N?

- A) $-2298 \hat{i} + 9 \hat{j}$
- B) $-126 \hat{i} - 9 \hat{j}$
- C) $-30 \hat{i} - 15 \hat{j}$
- D) $-186 \hat{i} - 15 \hat{j}$**
- E) $-2280 \hat{i} - 9 \hat{j}$

4) In a competition where participants of equal mass demonstrate their performance, the winner is determined by who can lift five cement bags, each weighing 40 kg, to a height of 1 m in the shortest time. Which physical quantity can be used to decide the winner?

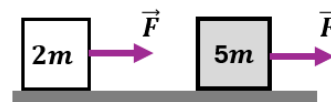
- A) The total energy transferred to the bags
- B) The physical work done
- C) The gravitational potential energy
- D) The power they generate**
- E) The ratio of the work done to the energy consumed

Questions 5-6

F forces are applied to two objects with masses $2m$ and $5m$, which are initially at rest on a frictionless horizontal surface as shown in figure.

5) What should the ratio $\Delta t_{2m}/\Delta t_{5m}$ of the durations of the forces' application be for the objects to have the same linear velocity?

- A) 2/5 B) 5/2 C) 3/5 D) 5 E) 1



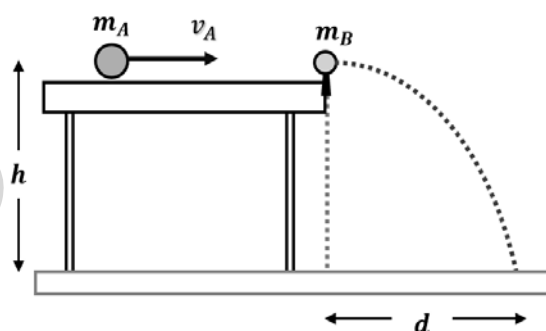
6) What should the ratio $\Delta t_{2m}/\Delta t_{5m}$ of the durations of the forces' application be for the objects to have the same kinetic energy?

- A) $2/\sqrt{5}$ B) $\sqrt{2}/\sqrt{5}$ C) 2/5 D) 5/2 E) $1/\sqrt{5}$

7) LABORATORY QUESTION

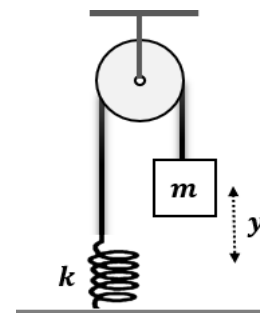
In a frictionless environment, a sphere A with a mass of 0.5 kg moves at 2.0 m/s on a horizontal plane and collides head-on with a stationary sphere B of mass 0.2 kg . After the collision, sphere A rebounds with a speed of 0.8 m/s in a straight line, while sphere B moves forward along the trajectory shown. If the height of the table from the ground is 5 cm , what is the horizontal distance d in cm ?

- A) 58 B) 28 C) 84 D) 30 E) 70



8) In the system shown, a spring with a force constant k is initially at its equilibrium position and then released. The pulley is frictionless. When the mass m descends vertically by a distance y , what is the velocity of m ?

- A) $\sqrt{gy - \frac{k}{m}y^2}$ B) $\sqrt{2gy - \frac{k}{m}y^2}$ C) $\sqrt{gy - \left(\frac{k}{m}\right)^2}$ D) $\sqrt{\frac{gy}{2} - \frac{2k}{m}}$ E) $\sqrt{gy - \frac{2k}{m}y^2}$

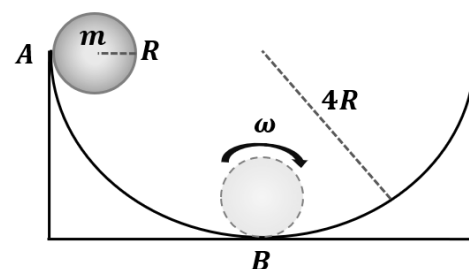


Questions 9-10

A glass marble with mass m and radius R starts rolling without slipping from point A at the top of a spherical bowl with radius $4R$.

9) What is the linear velocity of the marble as it passes point B at the bottom of the bowl?

- A) $\sqrt{30gR/7}$
 B) $\sqrt{40gR/7}$
 C) $\sqrt{50gR/7}$
 D) $\sqrt{60gR/7}$
 E) $\sqrt{10gR}$

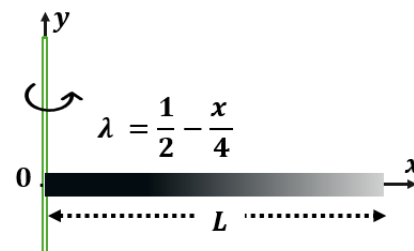


10) What is the kinetic energy of the glass marble at point B?

- A) $5/8 (mgR)$
- B) $5/4 (mgR)$
- C) $3 (mgR)$
- D) $7/3 (mgR)$
- E) $15 (mgR)$

Questions 11-14

A solid rod with a length of 1 m has a non-uniform linear mass density given by $\lambda = \frac{1}{2} - \frac{x}{4}$, where λ and x are expressed in $\frac{\text{kg}}{\text{m}}$ and m , respectively. Initially, the rod is stationary, and at $t = 0$, it begins to rotate with a constant angular acceleration of $\alpha = 4\text{ rad/s}^2$.



11) What is the moment of inertia of the rod about an axis passing through its denser end and perpendicular to its length in kg m^2 ?

- A) $5/16$
- B) $5/24$
- C) $11/48$
- D) $5/48$
- E) $5/36$

12) What is the rotational kinetic energy of the rod about the same axis at $t = 2\text{ s}$, in joules?

- A) $22/3$
- B) $10/3$
- C) 20
- D) 40
- E) $5/3$

13) What is the magnitude of the net torque acting on the rod about the same axis at $t = 2\text{ s}$, in Nm ?

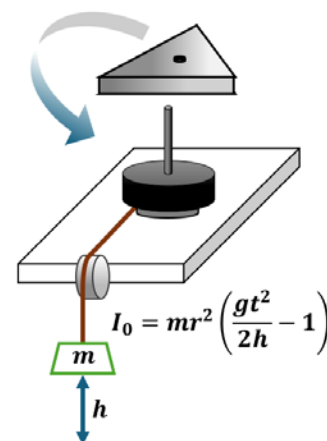
- A) $5/4$
- B) $5/6$
- C) $5/12$
- D) $11/12$
- E) $5/9$

14) What is the distance between the center of mass of the rod and its denser end at the initial moment, in meters?

- A) $8/9$
- B) $8/15$
- C) $4/9$
- D) $4/15$
- E) $4/5$

15) LABORATORY QUESTION

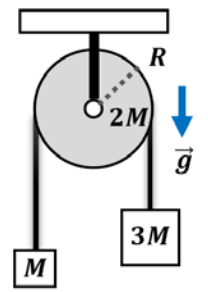
A setup to determine the moment of inertia using energy conservation includes a pulley with a radius $r = 2\text{ cm}$ attached under a reference table. A string is wound around the pulley, with a mass of 10 g attached to the string's end. The string passes over an massless and frictionless pulley and hangs vertically with mass m . When the system is released, the time it takes for m to fall a vertical distance $h = 100\text{ cm}$ is measured, and the reference table's moment of inertia is determined to be 760 g cm^2 . When a homogeneous equilateral triangular plate is placed on the reference table with its center of mass aligned with the rotation axis, it is found that m takes 5 s to travel the same distance. What is the moment of inertia of the equilateral triangular plate relative to its center of mass in g cm^2 ? (All frictional forces are neglected)



- A) 1200
- B) 2200
- C) 3200
- D) 4200
- E) 5200

Questions 16-17

Two objects with masses M and $3M$ are attached to the ends of a massless string passing over a pulley with a mass of $2M$, fixed to the ceiling. The string does not slip on the pulley, and the pulley can rotate frictionlessly around its axis.



16) What is the acceleration of the blocks?

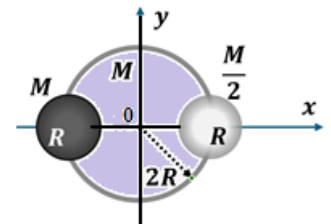
- A) $g/5$ B) $2g/3$ C) $3g/5$ D) $g/10$ E) $2g/5$

17) What is the T_1/T_2 ratio?

- A) $10/9$ B) $7/10$ C) $7/9$ D) $9/7$ E) 1

Questions 18-19

A solid disk with a mass M and radius $2R$ has two solid spheres attached at its edges, each with a radius R . The spheres, made from different materials, have uniform mass densities, with masses M and $M/2$, respectively.



18) What are the coordinates of the center of mass in terms of R ?

- A) $(-1/5, 0)$ B) $(0, 7/5)$ C) $(-2/5, 0)$ D) $(-3/5, 0)$ E) $(0, 2/5)$

19) What is the moment of inertia of the system about an axis passing through its center of mass, expressed in MR^2 ?

- A) $41/5$ B) $4/5$ C) $43/5$ D) $51/25$ E) $11/5$

20) On a frictionless inclined plane, an object m with a mass of 235 g , initially moves with a velocity of $v_i = 5\text{ m/s}$. As it travels a displacement x , its speed decreases by 2 m/s . What is the displacement of the object in m ?

- A) $6/5$
 B) $5/2$
 C) $21/10$
 D) $47/3$
 E) $8/5$

