

RECITATION 2

1) The radius r of a circle inscribed in any triangle whose sides are a , b , and c is given by $r = \left[\frac{(s-a)(s-b)(s-c)}{s} \right]^{1/2}$, where s is an abbreviation for $(a+b+c)/2$. Check this formula for dimensional consistency.

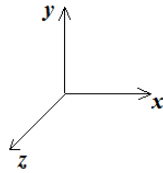
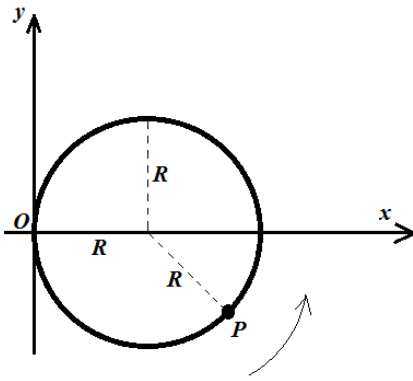
2) Check which of the following equations are dimensionally correct:

a) $\frac{mv^2}{2} = Ft$ (where m is the mass, v is the velocity, F is the force and t is the time)

b) $\frac{mv^2}{2} = Fd$ (where m is the mass, v is the velocity, F is the force and d is the displacement)

3) A force F acting on a body of mass m a distance r from some origin has magnitude $F = \frac{Ame^{-\alpha r}}{r^3}$, where A and α are both constants. The constant $e = 2,718\dots$. What are the dimensions of the constants A and α ? And determine the units of the constants A and α in SI system.

4)

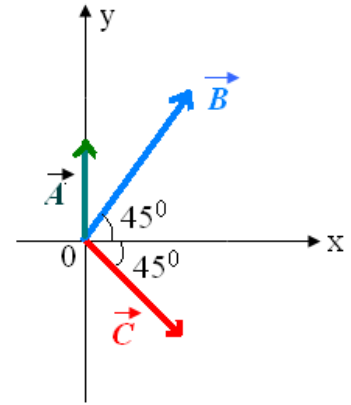


A particle P travels with constant speed v on a circle of radius R . The particle passes through O at time $t=0$ in counterclockwise direction and has a period T .

- a) With respect to O , find the particle's position vector at time $t = \frac{3T}{4}$. Give your result in terms of unit vectors.
- b) Calculate the scalar product $\vec{v} \cdot \vec{r}$ where \vec{v} and \vec{r} are, respectively, the velocity and position vectors of the particle at time $t = \frac{3T}{4}$.
- c) Calculate the vector product $\vec{a} \times \vec{r}$ where \vec{a} and \vec{r} are, respectively, the acceleration and position vectors of the particle at time $t = \frac{3T}{4}$. Give your result in terms of unit vectors.
- d) Where is the particle if $\vec{r} \cdot \vec{v} = 0$?
- e) Where is the particle if $\vec{a} \times \vec{r} = 0$?

5) Three vectors are oriented as shown in figure, where $|\vec{A}| = 20 \text{ m}$, $|\vec{B}| = 40 \text{ m}$ and $|\vec{C}| = 30 \text{ m}$. Find;

- The x and y components of the resultant vector,
- The magnitude and direction of the resultant vector.



6) A car travels 20 km east, then 10 km north, and then 40 km northeast (30° east of north). Draw a vector diagram and write the displacement vector from the starting point. Find the magnitude and direction of the displacement vector.